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## age distributions of the emigrants from Greece

1. introductory remarks

In many social phenomena the duration of some particular activities is a useful measure of behavior. Thus, for example, the length of human life or specially the age at migration as a measure of staying by an individual in a region is of fundamental interest to the researchers. Of course, such phenomena are subjected to a high degree of variability and furthermore to an appropriate stochastic analysis. From this point of view, we will try to study the migration process by comparing frequency distributions predicted by model-building with those observed in practice.

The length of life staying in a region or more generally the duration of staying in a social state ${ }^{1}$ can be studied in many cases analogously as in other areas outside the social sciences. The best known and most developed is the reliability theory and the industrial life testing. In spite of having important differences between the social and industrial applications according to the types of the distributions and collections of the data, ${ }^{2}$ we shall follow the terminology and notation given in the reliability theory.

The main variable T underlying to investigation denotes the age of the individuals migrated from a region. We assume that T gives the duration of staying in the concerned region, if an individual is born there. Apart from mentioned exceptions, $T$ will be continuous. Under these conditions, we can draw up a table of useful quantities that are objects of our main interest.
(a) The distribution function $F(t)$. This is the cumulative probability

$$
F(t)=P(T \leq t)
$$

an individual to stay in the concerned region until the age $t$.
(b) The survivor function $G(t)$. This is the complement of the distribution function $\mathrm{F}(\mathrm{t})$.
(c) The migration-age density function $f(t)$. This is an equivalent quantity to completed length of service density function (CLS-distribution) in life testing and it is defined as the density function associated with $F(t)$, related to the survivor function by

$$
\begin{equation*}
f(t)=-\frac{d G(t)}{d t} \tag{1.1}
\end{equation*}
$$

(d) The number of emigrants in time interval (t, $t+1)$ is defined by

$$
\begin{equation*}
\mathrm{n}[\mathrm{G}(\mathrm{t})-\mathrm{G}(\mathrm{t}+1)] \tag{1.2}
\end{equation*}
$$

where n denotes the total number of out-migrants.

[^0](e) The intensity function or failure rate $\lambda(t)^{3}$ can be defined as follows:
Prob $\{$ migration in $(\mathrm{t}, \mathrm{t}+\delta \mathrm{t}) /$ survival to t$\}=\lambda(\mathrm{t}) \delta \mathrm{t}$.
Furthermore we have
$\mathrm{f}(\mathrm{t})=\operatorname{Prob}\{$ migration in $(\mathrm{t}, \mathrm{t}+\delta \mathrm{t})\}$
$=$ Prob $\{$ survival to t$\}$ Prob $\{$ migration in ( t , $\mathrm{t}+\delta \mathrm{t}$ ) /survival to t$\}$.

Hence $\quad \lambda(t)=\frac{f(t)}{G(t)}=-\frac{d \log G(t)}{d t}$
or

$$
\begin{equation*}
G(t)=\exp \left\{-\int_{0}^{1} \lambda(x) d x\right\} \tag{1.3}
\end{equation*}
$$

(f) The specific rate of migration $r(t)$ at age $t$ can be defined as follows:

$$
\begin{equation*}
r(t)=\frac{G(t)-G(t+1)}{\int_{t}^{t+1} G(x) d x} \tag{1.5}
\end{equation*}
$$

## 2. age distribution of the temporary emigrants from Greece

Lane and Andrew in their notable contributions introduced the log-normal distribution to analyse the phenomenon of labour turnover. Afterwards their findings have been confirmed many times and have become a principal tool in manpower planning. Hence, we may also apply the same principle in the present context to deduce that the form of the age distribution tends to lognormality.

Let $\mathrm{T}_{\mathrm{j}}$ denotes the length of life time spent at least by an individual in a subregion j . If $\left\{\mathrm{u}_{2}, \mathrm{u}_{3}, \ldots,\right\}$ is a sequence of random variables with known joint distribution, then the migration-age T and the law states are

$$
\begin{gather*}
T_{i}=T_{j-1} u_{j} \quad(j=2,3, \ldots,)  \tag{2.1}\\
T=T_{i} u \tag{2.2}
\end{gather*}
$$

where u is a random variable.
Equation (2.1) and (2.2) may be regarded as expressions of the way that previously influences the future migration. An individual who has been staying for a long time in a region will tend to stay a long time in future.

An immediate consequence of equation (2.1) is that

$$
\mathrm{T}=\mathrm{u} \mathrm{~T}_{1} \prod_{\mathrm{i} \sim 2}^{1} \mathrm{u}_{\mathrm{i}} \quad(\mathrm{j} \geq 2)
$$

3. The intensity rate is known in the literature of reliability theory as hazard rate. In actuarial statistics the intensity rate goes under the name of mortality.
or

$$
\begin{equation*}
\log T=\log T_{1}+\log u+\sum_{i=2}^{j} \log u_{i} \tag{2.3}
\end{equation*}
$$

Provided that the joint distribution of the u's is such that the central limit theorem applies to the sum of their logarithms, it follows that $\log \mathrm{T}$ will tend to normality as j increases. Thus, the model predicts that a new emigrant who has been in several subregions in the past will have a migration-age density function which is approximately log-normal.
We assume further that $u_{i}(i=2,3, \ldots$,$) has the$ same joint distribution for all individuals of the population from which the migrants come. Under this condition, we can draw an important conclusion. Suppose that we classify all migrants according to the number of regions where they stayed in the past. Then, within these groups the model predicts that the standard deviation $\sigma$ of $\log \mathrm{T}$ should be constant. On the other hand, the mean m of $\log \mathrm{T}$ depends on the characteristics of the individuals through $\log \mathrm{T}_{1}$. Even if the groups are not homogeneous with respect to the number n of previous subregions the conclusion may still apply, because if the factors $u_{i}$ have mean near to one then $\operatorname{logu}_{i}$ will have mean near to zero. So that $\sigma$ will depend only slightly on $n$. Provided that n does not vary too much, the shape of the overall distribution is not likely to be seriously distorted by the effect which variation in n will have on $\sigma$.

The theory can go further, however, by supposing that these initial characteristics reflected in the quantities $\mathrm{T}_{1}$ can be modified by subsequent stay in another subregion. Even, if this explanation is only partly true, it has an important practical consequence. Equation (2.3) shows an important role played by length of life time spent in the first subregion on subsequent lengths of stay. This suggests that if particular care is taken to ensure satisfaction in a person's first stay then their subsequent rate of migration will be reduced. We note here that the existing data do not provide enough information to enable a satisfactory test about such a hypothesis to be made.

In order to apply these considerations to the temporary emigrants of Greece, first we need an estimation of the parameters. Thus, from the knowledge that T has a two parameter log-normal distribution, one can obtain estimates of m and $\sigma$ with optimum properties by considering the distribution $\mathrm{W}=\log \mathrm{T}$. The maximum-likelihood estimator $\hat{\mathrm{m}}$ of m is the sample mean given by

$$
\begin{equation*}
\frac{\sum_{k=1}^{v} f_{k} w_{k}}{v}=\frac{1}{v} \sum_{k=1}^{v} f_{k} \log _{k} \tag{2.4}
\end{equation*}
$$

where $t_{k}$ is the $k$ th ordered observable sample with frequency $f_{k}$ from a log-normal distribution and $v$ is
the sample size. The maximum-likelihood estimator $\hat{\sigma}^{2}$ of $\sigma^{2}$ is

$$
\begin{equation*}
\frac{1}{v} \sum_{k=1}^{v} f_{k}\left(\log t_{k}\right)^{2}-\frac{1}{v}\left[\sum_{k=1}^{v} f_{k} \log t_{k}\right]^{2} \tag{2.5}
\end{equation*}
$$

On the basis of observed data from tables (2.1), (2.2), (2.3) and (2.4) we calculated the parameters for the pertinent groups of the emigrants according to the marital status and for the total distribution. An estimation of the standard deviation is about the same equal to $\hat{\sigma}=0.3$. On the other hand we have estimated different values for the mean of the three groups. The fitted distributions and the whole results are illustrated in the mentioned tables with the observed distributions.
Having the form of the empirical distribution we can construct a second model on the basis of gamma distributions. Thus, let us assume now that the kth individual migrates from a region at time $T(k)$ and the time $\mathrm{T}_{\mathrm{i}}$ between $i$ th and ( $\mathrm{i}-1$ )th migration has an exponential distribution with a constant parameter $\lambda$. This is a similar consideration to the constant failure rate. The probability density function of the random variable $\mathrm{T}(\mathrm{k})$ is defined by the k -fold convolution of the $\mathrm{T}_{\mathrm{i}} \mathrm{s}$ as ${ }^{4}$
$f_{T(k)}(t)=\left[f_{T_{i}}(t)\right]^{k}=\int_{0}^{t}\left[f_{T_{i}}(t-s)\right]^{k-1} f_{T_{i}}(s) d s$
where

$$
f_{T_{i}}(t)=\lambda e^{-\lambda t} \quad(\lambda>0, t \geq 0)
$$

Accordingly

$$
\begin{aligned}
& {\left[f_{T_{i}}(t)\right]^{2}=\int_{0}^{t} f_{T_{i}}(t-s) f_{T_{i}}(s) d s=} \\
& \quad=\int_{0}^{t} \lambda^{2} e^{-(t-s)} e^{-t s} d s=\frac{\lambda^{2} t e^{-t \lambda}}{\Gamma(2)}
\end{aligned}
$$

In general, it can be deduced that

$$
\begin{equation*}
f_{T}(k)(t)=\left[f_{T_{i}}(t)\right]^{k}=\frac{\lambda^{k}}{\Gamma(k)} t^{k-1} e^{-\lambda t} \tag{2.8}
\end{equation*}
$$

which is the gamma probability density junction for $\mathrm{k} \geqslant 1$.
In order to apply the gamma distribution given by (2.8) to the temporary emigrants age-distribution in Greece, first we need an estimation of the two parameters. An efficient method of parameter estimation is that of maximum-likelihood. Thus, the maximum likelihood equations reduce to

[^1]\[

$$
\begin{gather*}
\left(\frac{\hat{1}}{\lambda}\right)=\frac{\sum_{k=1}^{v} f_{k} t_{k}}{v \hat{k}} \text { and } \\
\left.2 \hat{k} \simeq \log \left(\sum_{k=1}^{v} \frac{f_{k} t_{k}}{v}\right)-\frac{1}{v} \sum_{k=1}^{v} f_{k} \log t_{k}\right]^{-1}+\frac{1}{3} \tag{2.9}
\end{gather*}
$$
\]

where $t_{k}$ is the $k$ th ordered observable sample with frequency $f_{k}$ and $v$ is the sample size.

Alternatively, the method of moments can be employed for estimating $\lambda$ and k . Moment estimators, given by

$$
\begin{equation*}
\left(\frac{\tilde{1}}{\lambda}\right)=\frac{\sum_{k=1}^{v} f_{k} t_{k}}{v \tilde{k}} \quad \tilde{k}=\frac{\sum_{k-1}^{v} f_{k} t_{k}}{v \sum_{k=1}^{v} f_{k}\left(t_{k}-\bar{t}\right)^{2}} \tag{2.10}
\end{equation*}
$$

are obtained by equating $\mathrm{k}(1 / \lambda)$ and $\mathrm{k}(1 / \lambda)^{2}$ to the sample mean and the variance respectively. These estimators have a lower asymptotic efficiency than the corresponding maximum-likelihood estimators.

On the basis of the observed data from the tables (2.1), (2.2), (2.3) and (2.4) we calculated for the concerned three groups of the emigrants according to the marital status and for the total distribution of $\lambda$ and k by the method of moments.

## 3. age distribution for the permanent emigrants from Greece

Silcock (1954) published two empirical CLSdistribution obtained in his studies for different firms. His first model was based on a constant loss intensity that leads to an exponential CLS-distribution. It is doubtful whether Silcock's interpretation is justified, since the loss intensity could centainly depend on factors internal to the firm, including the individuals length of service. The second model proposed by Silcock is a generalization of the first. It retains the simple assumption of constant loss rate for individuals but this rate is now supposed to vary in the population from which employees are drawn. This is a very plausible hypothesis. Individuals differ almost from all other aspects of their behavior. In order to apply these considerations Silcock introduced an exponential CLS-distribution supposing that $\lambda$ is a random variable with a gamma distribution and calculated the compound distribution.

Now, for our application to the permanently emigrants from Greece, it is simpler to suppose that a constant loss intensity can be regarded at least for a group of the emigrants, who have a commom be-

TABLE 2.1. Observed and Fitted Age-distribution of the Temporary Emigrants from Greece: 1975 (males)*

| Age <br> (years) | Actual number <br> of out-migrants | Log-normal <br> fit | Gamma <br> fit |
| :---: | :---: | :---: | ---: |
| $0-4$ | - | 0 | 6 |
| $5-9$ | 12 | 4 | 46 |
| $10-14$ | 57 | 360 | 794 |
| $15-19$ | 9070 | 3298 | 3770 |
| $20-24$ | 11259 | 9507 | 8800 |
| $25-29$ | 16846 | 14438 | 13145 |
| $30-34$ | 10822 | 15086 | 14485 |
| $35-39$ | 9826 | 12442 | 12814 |
| $40-44$ | 7784 | 8847 | 9606 |
| $45-49$ | 5814 | 5696 | 6327 |
| $50-54$ | 3094 | 3435 | 3756 |
| $55-59$ | 1761 | 1982 | 2048 |
| $60-64$ | 831 | 1109 | 1041 |
| $65-69$ | 280 | 609 | 498 |
| $70-74$ | 55 | 330 | 226 |
| $75-79$ | 12 | 178 | 98 |
| $80-84$ | 1 | 95 | 41 |
| $>85$ | - | 111 | 26 |
| Total | 77527 | $\hat{m}=1,90629$ | $\hat{k}=10,286$ |
|  |  | $\hat{\sigma}=0,31093$ | $\hat{\lambda}=0,687$ |

*S o ur c e : Statistical Yearbook of Greece (1975).

TABLE 2.2. Observed and Fitted Age-distribution of the Temporary Emigrants from Greece: 1975 (males-single)*

| Age <br> (years) | Actual number <br> of out-migrants | Log-normal <br> fit | Gamma <br> fit |
| :---: | :---: | ---: | ---: |
| $0-4$ | - | 0 | 0 |
| $5-9$ | 12 | 0 | 21 |
| $10-14$ | 57 | 245 | 692 |
| $15-19$ | 8842 | 3404 | 4013 |
| $20-24$ | 10277 | 9706 | 8806 |
| $25-29$ | 11585 | 11402 | 10380 |
| $30-34$ | 4489 | 7950 | 7977 |
| $35-39$ | 2092 | 4111 | 4494 |
| $40-44$ | 1007 | 1693 | 2002 |
| $45-49$ | 597 | 627 | 742 |
| $50-54$ | 254 | 209 | 238 |
| $55-59$ | 149 | 75 | 67 |
| $60-64$ | 63 | 20 | 17 |
| $65-69$ | 23 | 8 | 4 |
| $70-74$ | 5 | 3 | 1 |
| $75-79$ | 1 | 0 | 0 |
| $80-84$ | 1 | 0 | 0 |
| $>85$ | 0 |  | 0 |
|  |  | 39454 | 39454 |
| Total | 39454 | $\hat{m}=1,71163$ | $\hat{k}=14,089$ |
|  |  | $\hat{\sigma}=0,28000$ | $\hat{\lambda}=0,406$ |

[^2]TABLE 2.3. Observed and Fitted Age-distribution of the Temporary Emigrants from Greece: $14^{-}$. (males-married)*

| Age <br> (years) | Actual number <br> of out-migrants | Log-normal <br> fit | Gamma <br> fit |
| :---: | :---: | :---: | :---: |
| $0-4$ | - | - | - |
| $5-9$ | - | - | - |
| $10-14$ | 224 | 0 | 0 |
| $15-19$ | 962 | 727 | 28 |
| $20-24$ | 5197 | 2813 | 548 |
| $25-29$ | 6236 | 6365 | 5771 |
| $30-34$ | 7644 | 7970 | 7810 |
| $35-39$ | 6709 | 7146 | 7576 |
| $40-44$ | 5111 | 5197 | 5774 |
| $45-49$ | 2794 | 3335 | 3669 |
| $50-54$ | 1585 | 1961 | 2023 |
| $55-59$ | 751 | 1095 | 996 |
| $60-64$ | 248 | 592 | 446 |
| $65-69$ | 48 | 314 | 185 |
| $70-74$ | 11 | 163 | 72 |
| $75-79$ | 0 | 175 | 45 |
| $>80$ | 37560 | 37560 | 37560 |
|  |  | $\hat{\mathrm{~m}}=1,81702$ | $\hat{\mathrm{k}}=11,168$ |
| Total |  | $\hat{\sigma}=0,31611$ | $\hat{\lambda}=0,576$ |
|  |  |  |  |

* S our c e : Statistical Yearbook of Greece (1975).

TABLE 2.4. Observed and Fitted Age-distribution of the Tempo, ary Emigrants from Greece: 1975 (males-divorced)*

| Age <br> (years) | Actual number <br> of out-migrants | Log-normal <br> fit | Gamma <br> fit |
| :---: | :---: | :---: | :---: |
| $0-4$ | - | - | - |
| $5-9$ | - | - | - |
| $10-14$ | - | 0 | 0 |
| $15-19$ | 1 | 0 | 0 |
| $20-24$ | 19 | 7 | 6 |
| $25-29$ | 57 | 39 | 40 |
| $30-34$ | 86 | 76 | 77 |
| $35-39$ | 80 | 88 | 94 |
| $40-44$ | 55 | 74 | 81 |
| $45-49$ | 53 | 51 | 54 |
| $50-54$ | 35 | 32 | 30 |
| $55-59$ | 12 | 18 | 14 |
| $60-64$ | 5 | 11 | 6 |
| $65-69$ | 1 | 6 | 2 |
| $70-74$ | 1 | 3 | 1 |
| $>75$ | 0 | 0 | 0 |
| Total | 405 |  | 405 |
|  |  | $\hat{m}=1,7787$ | $\hat{\mathrm{k}}=11,7147$ |
|  |  | $\hat{\sigma}=0,3242$ | $\hat{\lambda}=0,5313$ |

[^3]havior depended on their educational obligations. On the other hand we assume that the permanently emigrant in higher ages can be distributed by ages according to a log-normal or gamma law in the same way as the temporary emigrants. If the associated probabilities are $\mathrm{a}_{1}$ and $1-\mathrm{a}_{1}$ respectively the distribution will be according to the first model
$f(t)=a_{1} \lambda_{1} e^{-\lambda_{1} t}+\left(1-a_{1}\right) \frac{1}{\sqrt{2 \pi} \sigma} \exp \left\{-\frac{(\log t-m)^{2}}{2 \sigma^{2}}\right\}$
and by the second model
$$
f(t)=a_{1} \lambda_{1} e^{-\lambda_{1} t}+\left(1-a_{1}\right) \frac{\lambda_{2}^{k}}{\Gamma(k)} x^{k-1} e^{-\lambda_{2} x}
$$

These models are two-term mixed distribution and are fitted to the data given by the National Statistical Service of Greece. For estimating the parameters of such mixed models, several graphical and theoretical methods have been proposed. For our models we assume that $a_{1}=0,1$ or $10 \%$ of the total emigrants will be distributed by age according to a constant intensity failute rate. This group must be the young individuals of the migrated population. From this reason we can take an estimation of the parameter $\lambda_{1}$
having only the first age group, that is distributed according to the exponential law. Thus, we have $\hat{\lambda}_{1}=$ 0.7199 .

In table (3.1), we illustrated the whole results about the fitted log-normal and gamma distributions having estimators for the parameters given by the relationships (2.4), (2.5) and (2.9).

According to the marital status of the emigrants we calculated again estimators for the parameters of the distributions considering the same hypothesis about the distribution of young individuals. Thus, for unmarried permanent emigrants, we assume that $10 \%$ or 1171 individuals are distributed according to the exponential law and the rest according to the lognormal or gamma law. For the two other groups we have not any problem because we take emigrants only in higher ages. The whole results are illustrated in table (3.2), (3.3) and (3.4).

Although the models described above are in good agreement with the data, it cannot be concluded from the foregoing analysis that mixed models provide a true explanation of the migration process. On the other hand the models suggest that we can find ways for discriminating between emigrants according to their propensity to leave. But, this is another problem more concerned to a further sociological analysis.

TABLE 3.1. Observed and Fitted Age-distribution of the Permanent Emigrants from Greece: 1975 (males)*

| $\begin{gathered} \text { Age } \\ \text { (years) } \end{gathered}$ | Actual number of outmigrants | Exponential fit | $\underset{\text { fit }}{\text { Log-normal }}$ | A mixed model | $\underset{\text { fit }}{\text { Gamma }}$ | B mixed model |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0-4 | 601 | 601 | 0 | 601 | 0 | 601 |
| 5-9 | 532 | 293 | 10 | 303 | 36 | 329 |
| 10-14 | 353 | 142 | 211 | 353 | 274 | 416 |
| 15-19 | 1326 | 69 | 848 | 917 | 795 | 864 |
| 20-24 | 1590 | 34 | 1535 | 1569 | 1371 | 1405 |
| 25-29 | 1954 | 16 | 1817 | 1833 | 1706 | 1722 |
| 30-34 | 1364 | 8 | 1689 | 1697 | 1710 | 1718 |
| 35-39 | 1337 | 4 | 1357 | 1361 | 1464 | 1468 |
| 40-44 | 996 | 2 | 995 | 997 | 1115 | 1117 |
| 45-49 | 726 | 1 | 689 | 690 | 775 | 776 |
| 50-54 | 339 | 1 | 459 | 460 | 500 | 501 |
| 55-59 | 183 | 0 | 298 | 298 | 393 | 393 |
| 60-64 | 150 | 0 | 191 | 191 | 176 | 176 |
| 65-69 | 79 | 0 | 121 | 121 | 97 | 97 |
| 70-74 | 48 | 0 | 76 | 76. | 52 | 52. |
| 75-79 | 14 | 0 | 48 | 48 | 27 | 27 |
| 80-84 | 5 | 0 | 30 | 30 | 14 | 14 |
| >85 | 2 | 0 | 54 | 54 | 13 | 13 |
| Total | 11599 | 1171 | $\begin{array}{r} 10428 \\ \hat{\mathrm{~m}}=1,86408 \end{array}$ | 11599 | $\begin{array}{r} 10428 \\ \hat{\mathrm{k}}=7.5840 \end{array}$ | 11599 |
|  |  | $\hat{\lambda}_{1}=0,7199$ | $\hat{\sigma}=0,37691$ |  | $\hat{\lambda}_{2}=0,9097$ |  |

[^4]TABLE 3.2. Observed and Fitted Age-distribution of the Permanent Emigrants from Greece: 1975 (males-single)*

| $\begin{gathered} \text { Age } \\ \text { (years) } \end{gathered}$ | Actual number of outmigrants | Exponential fit | $\underset{\text { fit }}{\log \text {-normal }}$ | A mixed model | Gamma fit | B mixed model |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0-4 | 601 | 601 | 0 | 601 | 0 | 601 |
| 5-9 | 532 | 293 | 18 | 311 | 38 | 331 |
| 10-14 | 353 | 142 | 325 | 467 | 332 | 474 |
| 15-19 | 1301 | 69 | 937 | 1006 | 851 | 920 |
| 20-24 | 1339 | 34 | 1144 | 1178 | 1115 | 1149 |
| 25-29 | 917 | 16 | 903 | 919 | 958 | 974 |
| 30-34 | 273 | 8 | 559 | 567 | 620 | 628 |
| 35-39 | 144 | 4 | 304 | 308 | 327 | 331 |
| 40-44 | 92 | 2 | 153 | 155 | 148 | 150 |
| 45-49 | 48 | 1 | 74 | 75 | 59 | 60 |
| 50-54 | 19 | 1 | 35 | 36 | 22 | 23 |
| 55-59 | 11 | 0 | 16 | 16 | 7 | 7 |
| 60-64 | 13 | 0 | 7 | 7 | 2 | 2 |
| 65-69 | 5 | 0 | 3 | 3 | 1 | 1 |
| 70-74 | 1 | 0 | 1 | 1 | 0 | 0 |
| $>75$ | 2 | 0 | 1 | 1 | 0 | 0 |
| Total | 5151 | 1171 | 4480 | 5651 | 4480 | 5651 |
|  |  |  | $\hat{\mathrm{m}}=1,57484$ |  | $=9,5317$ |  |
|  |  | $\hat{\lambda}_{1}=0,7199$ | $\hat{\sigma}=0.33355$ |  | $=0.5345$ |  |

* S o ur c e : Statistical Yearbook of Greece (1975).

TABLE. 3.3. Observed and Fitted Age-distribution of the Permanent Emigrants from Greece: 1975 (males-married)*

| Age <br> (years) | Actual number <br> of out-migrants | Log-normal <br> fit | Gamma <br> fit |
| :---: | :---: | :---: | :---: |
| $0-4$ | - | - | - |
| $5-9$ | - | - | - |
| $10-14$ | - | 0 | 0 |
| $15-19$ | 24 | 3 | 16 |
| $20-24$ | 250 | 115 | 158 |
| $25-29$ | 1023 | 581 | 554 |
| $30-34$ | 1071 | 1101 | 997 |
| $35-39$ | 1172 | 1238 | 1188 |
| $40-44$ | 895 | 1034 | 1072 |
| $45-49$ | 662 | 722 | 792 |
| $50-54$ | 318 | 252 | 502 |
| $55-59$ | 167 | 148 | 283 |
| $60-64$ | 129 | 80 | 145 |
| $65-69$ | 64 | 43 | 69 |
| $70-74$ | 40 | 23 | 31 |
| $75-79$ | 9 | 12 | 13 |
| $80-84$ | 4 | 12 | 5 |
| $>85$ | 0 |  | 5828 |
| Total | 5828 | $\hat{a}=1,77419$ | $\hat{\mathrm{k}}=9,4379$ |
|  |  | $\hat{a}=0,33010$ | $\hat{\lambda}=0,6592$ |

*S o u r c e : Statistical Yearbook of Greece (1975).

TABLE 3.4. Observed and Fitted Age-distribution of the Permanent Emigrants from Greece: 1975 (males-divorced)*

| Age (years) | Actual number of out-migrants | $\underset{\text { fit }}{\text { Log-normal }}$ | Gamma fit |
| :---: | :---: | :---: | :---: |
| 0-4 | - | - | - |
| 5-9 | - | - | - |
| 10-14 | - | - | - |
| 15-19 | 1 | 0 | 0 |
| 20-24 | 1 | 1 | 0 |
| 25-29 | 9 | 6 | 2 |
| 30-34 | 18 | 28 | 12 |
| 35-39 | 17 | 13 | 22 |
| 40-44 | 7 | 9 | 19 |
| 45-49 | $10^{\prime}$ | 6 | 10 |
| 50-54 | 1 | 3 | 3 |
| 55-59 | 1 | 2 | 1 |
| 60-64 | 2 | I | 0 |
| 65-69 | 1 | 0 | 0 |
| $70-74$ | 1 | 0 | 0 |
| $>75$ | 0 | 0 | 0 |
| Total | 69 | 69 | 69 |
|  | $\begin{aligned} \hat{\mathrm{m}} & =1.77536 \\ \hat{\mathrm{a}} & =0.31435 \end{aligned}$ |  | $\begin{aligned} & \hat{\mathbf{k}}=23.731 \\ & \hat{\lambda}=0.254 \end{aligned}$ |

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[^0]:    1. As a well known example can be regarded the phenomenon of labour turnover.
    2. Bartholomew (1973).
[^1]:    4. Feller, 1966, p. 45.
[^2]:    *S o u r c e : Statistical Yearbook of Greece (1975).

[^3]:    * S o u r c e : Statistical Yearbook of Greece (1975).

[^4]:    * Source : Statistical Yearbook of Greece (1975).

