Δελτίο της Ελληνικής Γεωλογικής Εταιρίας, τόμος L, σελ. 1184-1193 Πρακτικά 14ου Διεθνούς Συνεδρίου, Θεσσαλονίκη, Μάιος 2016

EARTHQUAKE HAZARD ALONG THE WESTERN COAST OF SOUTH AMERICA INFERRED FROM CONDITIONAL PROBABILITIES

Koravos G.¹, Vougiouka G.², Tsapanos T.M.¹, Drakatos G.³ and Olasoglou E.¹

¹Aristotle University of Thessaloniki, Department of Geology, 54124, Thessaloniki, Hellas, tsapanos@geo.auth.gr, gkoravos@sch.gr, eolaso@geo.auth.gr

²Georgia E. Vougiouka, Department of Mathematics, Aristotle University of Thessaloniki, 54124 T hessaloniki, HELLAS, georgiavuk@hotmail.com

³National Observatory of Athens, Institute of Geodynamis, Thision, 11810, Athens, Hellas, g.drakat@noa.gr

Abstract

The conditional probabilities method is considered to be an alternative approach in order to estimate the earthquake hazard. For this purpose, this technique was applied to the western side of South America, one of the most seismogenic regions of the world. The method is applied in six pre-determined zones which covered the whole examine area. The occurrence of the earthquakes as a function of time was assessed, using the conditional probabilities technique. The Kolmogorov-Smirnov test was applied in order to determine the distribution followed by the inter-arrival times between the successive past events. The test shows that the lognormal is the best fit distribution, for the scope of the present work.

The obtained results are in good accordance to the method applied. High probabilities are estimated for events with $Mw \ge 7.0$. For the whole western part of South America, there is a probability about 64% for an earthquake occurrence with magnitude $M \ge 8.0$, during a time period of 20 years. Higher probability ($\approx 73\%$) was estimated for a time period of 50 years and for an earthquake of magnitude $M \ge 8.5$. This is clearly showed for the event of 1960, where the next (a posteriori procedure) earthquake of M=8.8 occurred on 2010.

Keywords: conditional probability, Kolmogorov-Smirnov test, lognormal distribution, seismic zones, South America.

Περίληψη

Η εκτίμηση των υπό συνθήκη πιθανοτήτων στη σεισμολογία θεωρείται μία εναλλακτική προσέγγιση του υπολογισμού της σεισμικότητας μίας περιοχής. Η μέθοδος εφαρμόσθηκε στις δυτικές ακτές της Νότιας Αμερικής η οποία θεωρείται ως μία από τις πλέον σεισμογενείς περιοχές της Γης. Η υπό έρευνα περιοχή είχε χωρισθεί σε έζι ζώνες από προηγούμενες μελέτες και σε αυτές έγινε η εφαρμογή της μεθοδολογίας. Η έκλυση των σεισμών σε σχέση με τον χρόνο γένεσής τους υπολογίσθηκε χρησιμοποιώντας την μέθοδο των πιθανοτήτων υπό συνθήκη. Το στατιστικό τεστ των Kolmogorov-Smirnov εφαρμόσθηκε για να καθορισθεί η στατιστική κατανομή που ακολουθούν οι ενδιάμεσοι χρόνοι μεταξύ διαδοχικών σεισμών που συνέβησαν στο παρελθόν. Το τεστ έδειζε ότι η πλέον ενδεδειγμένη κατανομή για την παρούσα μελέτη είναι η λογαριθμοκανονική. Υπολογίσθηκαν υψηλές τιμές πιθανοτήτων για γένεση σεισμών με μεγέθη $M \ge 7.0$. Επίσης βρέθηκε για όλη την υπό μελέτη περιοχή πιθανότητα 64% για γένεση σεισμού με μέγεθος $M \ge 8,0$ κατά την διάρκεια των 20 επόμενων ετών. Υψηλότερη είναι η πιθανότητα για γένεση σεισμών με μεγέθη $M \ge 8.5$ που εκτιμήθηκε στο 73% τα επόμενα 50 χρόνια. Στην τελευταία περίπτωση υπήρζε η σύμπτωση των θεωρητικών αποτελεσμάτων με την πραγματικότητα αφού 50 χρόνια μετά την γένεση του σεισμού του 1960 (M9.5), δηλαδή το 2010, συνέβη σεισμός με μέγεθος M = 8.8.

Λέξεις κλειδιά: υπό συνθήκη πιθανότητα, Kolmogorov-Smirnov τεστ, λογαριθμοκανονική κατανομή, σεισμικές ζώνες, Νότια Αμερική.

1. Introduction

South America is one of the most seismically active regions of the world. Especially, Chile and Peru were ranked in the second and the forth position, respectively, among fifty seismogenic countries of the world, in terms of their seismicity (Tsapanos and Burton, 1991).

The reason for the high seismicity level and other associated phenomena (e.g. deformation) is related to the lithospheric process of the region. Nazca plate seems to be of complicated tectonic structure (Bilek, 2010) and is subducting underneath the South America plate. The seismic activity is mostly concentrated along the coasts of the Pacific Ocean, where the subduction process takes place and reverse faulting dominates the tectonic regime (Suarez *et al.*, 1990). The relative velocity of the convergence is about 9.3 cm/yr (Casaverde and Vargas, 1984), while there were referred velocities like 8.5 cm/yr (Quezada, 1997) and 9.0 cm/yr (Dewey and Lamb, 1992). The main characteristic of the area is the generation of large to great earthquakes like the widely known event of 1960 with moment magnitude M_w =9.5. Very large earthquakes were referred or recorded since historical era up to now at the interface between the two plates. Descriptions back to 16th century provide information about very large shocks (e.g. the event of 1570 in Conception or the one of 1687 in Ica). The magnitudes and the return periods (100-150 years) of such events indicate that most of the 90% of the deformation, caused by the relative motion at the interface of the two plates, is released by earthquakes (Kelleher, 1972; Prince and Scheweller, 1978; Stein *et al.*, 1986, Tsapanos and Christova, 2000).

Conditional probabilities can be considered as the quantity which allows the estimation of the likelihood that a region or an active fault is prone for the occurrence of a large event. McCann *et al.* (1979) stated a number of criteria in order to categorize the seismic potential. Later on, Nishenko and McCann (1981) used some tectonic and temporal criteria in order to estimate seismic potential for large earthquakes generation along segments of some major plate boundaries of the globe. Based on seismic potential technique, Nishenko (1985) estimated a probability of 59% for the occurrence of an earthquake of M \geq 7.5 along Chile. His estimation was verified by the occurrence of Valparaiso (Chile) earthquake (during 1985 with M=7.8). Nishenko (1991) estimated the seismic potential for plate boundary segments around the Pacific rim in terms of conditional probabilities, in order to find large earthquakes occurrence during the forthcoming years. Moreover, Tsapanos (2001) proposed the seismic zone and the magnitude interval (M \geq 7.8) of the 2001 earthquake (near coast of Peru), by the application of a Markov - chain process. The probability estimated for this particular shock was about 65%.

The paper confines itself to the reappraisal of the earthquake hazard along the western coast of South America, in terms of conditional probabilities.

2. Data used

The present study focuses in six pre-determined (Tsapanos, 2001) seismic zones (Fig. 1). These zones almost coincided with the zones defined by other researchers (Papadimitriou, 1993; Galanis *et al.*, 2001).



Figure 1 - Map of earthquake epicentres along the western side of the South America, is shown. The six zones considered are also revealed.

The initial data set (M \geq 6.5) for South America's shocks was extracted from the data bank of NEIC. The data are restricted only to shallow earthquakes. The catalogue is free of depended events, like fore – and aftershocks, by applying the method proposed by Musson (2000). Due to the high seismicity of the area, the final catalogue adopted includes only large earthquake (M \geq 7.0). The magnitude of the events in the catalogue is expressed as moment magnitude, M_w. In several cases, especially for historical and/or older earthquakes, the magnitudes were estimated as surface magnitudes, Ms. In such cases the Ms earthquake magnitudes were converted into Mw applied for this purpose the relation introduced by Scordilis (2006). The number of the data in each zone and their time interval, the mean and the standard deviation are listed in Table 1.

ZONE	Number of data	Time period of data	μ	σ
1	13	1797-2013	0.186	0.656
2	11	1619-2007	1.007	1,520
3	15	1604-2001	0.549	1.064
4	21	1796-1995	0.538	1.162
5	13	1575-1985	0.515	1.145
6	18	1570-2010	0.798	1.384

Table 1 - The number of the data used and the time period for which data are available in each one of the six zones examined. The mean μ and the standard deviation σ for each zone is tabulated, as well.

It is obvious that in each zone the data set includes both historical and instrumental events. It is interesting that the percentage of historical events varies from 47% (zone 3) to 62% (zone 5). The use of numerous historical events enriches the final data set at each zone and so the results are more precise.

3. The method applied

Several approaches exist concerning the estimation of the probability of recurrence of large earthquakes. The most important are the random and the conditional probability models.

The random model assumes that the recurrence time of an earthquake is randomly distributed. It adopts the Poisson distribution, where the probability of recurrence of an earthquake event is independent of the time elapsed since the last event.

The model of conditional probability for the earthquake recurrence assumes that there is dependence between the probability of recurrence and the time elapsed since the large previous earthquake.

In order to use the model of conditional probability, it is proved that the time t of an earthquake event approximates the lognormal distribution better than the normal distribution. For this aim, the Kolmogorov-Smirnov test (K-S test) is applied. The test compares the sample of each zone with the reference probability function. In the case of normal distribution, the K-S test compares the sample of each zone with the standard normal distribution and the null hypothesis that the sample follows this distribution is rejected. In the case of lognormal distribution, knowing that if the time t follows the lognormal distribution, the log(t) is normally distributed, the K-S test compares the logarithms of data for each one of the six zones with the standard normal distribution and the null hypothesis is accepted. All the tests were done at level a=0.10.

Equation 1 - Formula for the probability density function of t:

$$f(t) = \frac{1}{t\sigma\sqrt{2\pi}} \exp\left[-\frac{\left(\ln t - \mu\right)^2}{2\sigma^2}\right]$$
(1)

where, the parameters denoted as μ and σ are the mean and the standard deviation, respectively, of the logarithm's variables, which means

Equation 2 - Formula for the transformation of the log-normal distribution to standard normal:

$$X = e^{\mu + \sigma Z} \tag{2}$$

where, X is random variable, Z is a standard normal variable. Both parameters μ and σ are portrayed in Table 1.

In order to estimate the probability of recurrence of an earthquake, we estimate the conditional probability within a given time interval from t_0 to $t+t_0$. This conditional probability equals to:

Equation 3 - Formula for the conditional probability:

$$P(E) = \frac{F(t_0 + t) - F(t_0)}{1 - F(t_0)}$$

where, F(t) is the cumulative distribution function of the variable t and can be expressed as the integral of its probability density function f(x) as follows:

(3)

Equation 4 - Formula for the probability density function f(x)**:**

$$F(x) = \int_0^x f(t) dt$$
(4)

From the equation (3) the conditional probability is estimated, for the given time interval from t_0 to $t+t_0$ presupposing that no earthquake happened after the last prescribed event.

Fig. 2 delineates that the probability depends on the shape of the curve (μ and σ values) and of course to the width of the time window t. It is obvious that the conditional probability is rising up as the time window is widening.





The data of the six zones, as well as for the whole South America, follow this distribution in a lower or higher degree.

4. Results and Discussion

In Fig. 3 the plots of the conditional probabilities against the time for the six zones are presented. As it is depicted in Fig. 3 the shape of the distribution of these probabilities in time depends on the values of the standard deviation σ (http://en.wikipedia.org/wiki/Log-normal_distribution). A demonstration of the Cumulative Distribution Function, CDF (where μ =0) is presented in Fig. 4, from which it is revealed that the values of σ play a key role in the drawing of the distribution. For instance, when the value of σ is equal to 1/8 (0.125) the shape became very sharp (S-shape), e.g. zone 5.



Figure 3 - The conditional probability of an earthquake inter-event time is shown, during a specific time period for the six zones considered, along the western part of South America.

The conditional probabilities seem very high for all time periods (e.g. for zone 1 and for the magnitudes M \geq 7.0). As it is depicted in Fig.3 the conditional probabilities for magnitudes M \geq 7.5 and M \geq 7.8, are higher than the one of M \geq 7.0 in a time period of 8 and 6 years, respectively. Despite the values of σ , this can be interpreted if the probabilities of M \geq 7.0 would be estimated for longer time periods (e.g. 20 years). Very large earthquakes occurred in this zone in 1797 (M=8.3), in 1906 (M=8.8), 1958 (M=7.8), 1979 (M=8.1), as the last one generated in 2013 (M=7.0). The event of 1906 ruptured a segment of about 500 Km long (Kanamori and McNally, 1982).



Figure 4 - Cumulative Distribution Function for various values of standard deviation (σ) and the value of mean μ =0 (http://en.wikipedia.org/wiki/Log-normal_distribution). We added the curve (dark black) according to the obtained outputs σ =0.076 and μ ≈0.

In zone 2, the estimated conditional probabilities are low, exceed only the 50% (for M \geq 7.0), in a time period of 50 years. Lower probabilities (44% and 33%) are also observed and for the other two magnitude ranges M \geq 7.5 and M \geq 7.8, respectively. They illustrate an ordinary distribution in time. The very large earthquakes in this zone are: 1619 (M=8.6), 1746 (M=8.7) in 1960 (M=7.8), 1970 (M=7.9) and the last one in 2007, with M=8.0. For a 10 years time period and for M \geq 7.5 a low conditional probability was estimated (10.3%), while Nishenko (1991) estimated as 13% for the same time period.

Ordinarily distribution is also observed in zone 3. High conditional probabilities (70.5%), in a time period of 50 years, is calculated for earthquakes of M \geq 7.0. Slightly lower probabilities of 60% are observed for magnitudes M \geq 7.5 and definitely lower about 43.5% for magnitudes M \geq 7.8. Very large earthquakes occurred in this zone since the historical epoch: 1604 (M=8.5), 1615 (M=8.8) in 1687 (M=8.7), 1831 (M=7.8), 1868 (M=9.0) 1877 (M=8.3), 1942 (M=8.2) and the last one is in 2001 (M=8.4). Nishenko (1985) suggested conditional probabilities of 20%, for the next 10 years and for large earthquakes. Comparable results were estimated in the present study, where the conditional probability is about at 16.5% level for a 10-years time window.

An unregulated distribution is depicted in zone 4. Statistically, it behaves like the distribution of zone 1. Very high values are observed for the conditional probabilities, which reached the 90%, in a time period of 50 years and for M \geq 7.5. The probabilities are slightly lower (83%) for the earthquakes of magnitude M \geq 7.0 in a time period of 50 years. This lower pattern is observed from the beginning of the time period up to its end. Conditional probability reached the value of 58% for earthquakes of magnitude M \geq 7.8 in a time period of 50 years. The very large earthquakes reported in this zone are: 1819 (M=8.3), 1918 (M=7.9), 1922 (M=8.5), 1946 (M=7.9), 1966 (M=7.8) and 1995 (M=8.0).

Zone 5 is of special interest because for magnitude level $M \ge 7.8$ it shows an abnormal distribution. The conditional probabilities estimated are of intermediate values (58.3%, for $M \ge 7.0$), in a time period of 50 years, while a bit lower (50%) are the probabilities estimated for the magnitude range of $M \ge 7.5$. Both exhibit an ordinary distribution in time. The very large earthquakes of this zone occurred in: 1730 (M=8.7), 1822 (M=8.5), 1906 (M=8.2) and 1985 (M=8.0). The number of

earthquakes that occurred during the historical era is predominant ($\approx 60\%$) in this zone. This could be one of the reasons that the earthquakes having magnitudes M \geq 7.8 show this kind of distribution. The time interval is generally long (\geq 35 years) and the conditional probabilities are more reliable for long time periods (Fig. 5). Fig.5a shows the distribution for short time period (50 years), while Fig. 5b illustrates the same distribution for longer time-window (150 years). Historical records, concerning the very large earthquakes, point out that the recurrence time period along the examined area is larger than 60 years (Kelleher, 1972). According to Nishenko (1991) the average recurrence time for this zone is 95±10 years. But as it is aforementioned the values of σ is the key of the shape of the distribution. For the zone the calculated value is μ =-0.0019, which practically is zero or tend to zero and σ =0.076. Based on these values we set on Fig. 4 the new curve (in dark black), in order to compare the obtained σ value given that the μ value is practically the same, (tends to zero). The new curve fits much better to those values with σ less than 0.125. So we conclude that indeed σ controls the shape of the conditional probability curve.



Figure 5 - The conditional probabilities of zone 5 and for magnitude interval M≥7.8 are shown: a) for a range up to 50-years time period, and b) for a range up to150-years time period.

Zone 6 seems to be the active seismogenic part of the examined area and more specifically during the historical epoch, given that about 70% of the very large earthquakes along the western coast of South America occurred in this zone. The estimated conditional probabilities are high 67.3% (for $M \ge 7.0$), in a time period of 50 years. Lower probabilities (61.2% and 50.8%) are also observed and for the other two magnitude ranges $M \ge 7.5$ and $M \ge 7.8$, respectively. The very large earthquakes in this zone are: 1570 (M=8.3), 1575 (M=8.5), 1647 (M=8.5), 1657 (M=8.0), 1751 (M=8.5), 1835 (M=8.2), 1837 (M=8.0), 1914 (M=8.2), 1960 (M=9.5) and the last one occurred in 2010 with M=8.8. Conditional probabilities for time periods of 10, 20, 30, 40 and 50 years, for earthquakes with magnitude $M \ge 7.0$ in the six zones in which South America was divided, are listed in Table 2. Conditional probabilities in time are also estimated for earthquakes ranged in magnitudes $M \ge 8.0$ and $M \ge 8.5$ (Table 3).

Numerous earthquakes of such magnitudes occurred along the entire western coast of South America. The area is very productive in such events and already three earthquakes occurred during the present century (2001 M=8.4, 2007, M=8.0 and 2010 M=8.8).

Years /Zones	10	20	30	40	50
1	22.62	59.30	79.65	89.54	94.40
2	18.81	31.70	41.10	48.30	54.01
3	24.77	42.30	54.74	63.78	70.52
4	38.15	58.48	70.55	78.25	83.44
5	18.48	32.41	43.14	51.58	58.33
6	26.32	42.75	53.70	61.51	67.34

Table 2 - Conditional probabilities estimated for earthquakes with M≥7.0 in each zone for the next 10, 20, 30, 40 and 50 years from the present time.

Table 3 - The conditional probabilities estimated of earthquakes with magnitudes M≥8.0 and
M≥8.5, along the western side of South America. The estimations are for the next 10, 20, 30,
40, 50 and 100 years, from the present time.

Time Periods	M≥8.0 (%)	M≥8.5 (%)
10	38.25	17.19
20	62.77	37.75
30	76.41	53.70
40	84.34	65.25
50	89.19	73.53
100	97.52	91.70

Due to these shocks, low conditional probabilities are computed for the next 10-years. The probabilities are high during the next 30 years. It is very interesting that the "recent" earthquake of 2010 (M=8.8) occurred fifty years after the 1960 (M=9.5) earthquake, the largest event of the world up to now. The conditional probability along the west side of South America for a 50-years time window and for earthquakes with M≥8.5 is estimated equal to 73.5%.

5. Conclusions

It is widely known that an earthquake is the result of the strain energy released in a location, which originates a seismic slip in the collision of two lithospheric plates. This energy is accumulated in the interface of two plates for tens or hundreds of years and depends, between others, on the velocity of the under-thrusting plates. Slow and fast collision velocities reflect to longer or shorter recurrence time for an earthquake, respectively. The inter-event time of earthquakes as a function of time, as well as their recurrence time were assessed, using the conditional probabilities technique. This technique was applied in six pre-determined zones along the western side of South America, one of the most seismogenic regions of the world, due to the collision between Nazca and South America plates. In two of them (zones 4 and 5) some abnormalities observed showed that greater events have greater probability of inter-event time. This may due to the quality of the data because we have greater number of large earthquake during the historic epoch than in present era (20th and 21st century). As a general conclusion we can say that the results of the detailed analysis of the last event inter-event time show that the technique of the conditional probability seems to be a more advanced methodology and considered as a useful tool for the earthquake hazard mitigation. It is interesting that zone 1 showed the highest conditional probabilities for an earthquake occurrence with magnitude, Mw ≥7.0. During the review process of the present paper and specifically on 16th of April 2016, an earthquake with Mw=7.8 struck the coastal region of this zone, given that the previous event with Mw>7.8 occurred during 1979 (\approx 40 years). For this time span the estimated conditional probability is about 90% (Table 2).

6. References

- Bilek, S.L., 2010. Seismicity along the South American subduction zone: Review of large earthquakes, tsunamis and subduction zone complexity, *Tectonophysics*, 495(1-2), 2-14.
- Casaverde, L.A. and Vargas, J.N., 1984. Seismic risk in Peru, *Proc. Of the 8th world conference on earthquake engineering*, I, 93-100, July 21-28, San Francisco California U.S.A.
- Dewey, J.F. and Lamb, S.H., 1992. Active tectonics in Andes, Tectonophysics, 205, 79-95.
- Galanis, O.Ch, Tsapanos, T.M., Papadopoulos, G.A. and Kiratzi, A.A., 2001. An alternative Bayesian statistics for probabilistic earthquake prediction in Mexico, Central and South America, *Bull. Geol. Soc. Greece*, XXXIV/4, 1485-1491, http://en.wikipedia.org/wiki/Lognormal_distribution.
- Kanamori, H. and McNally, K.C., 1982. Variable rupture model of the subduction zone along the Ecuador-Columbia coast, *Bull. Seismol. Soc. of Am.*, 72(4), 1241-1253.
- Kelleher, J.A., 1972. Rupture zones of large south American earthquakes and some predictions, *J. Geophys. Res.*, 77, 2087-2103.
- McCann, W.R., Nishenko, S.P., Sykes, L.R. and Krause, J., 1979. Seismic gaps and plate tectonics: Seismic potential for major boundaries, *Pageoph.*, 117, 1082-1147.
- Musson, R.M.W., 2000. Generalised seismic hazard maps for the Pannonian Basin using probabilistic methods, *Pageoph.*, 157(1/2), 147-169.
- Nishenko, S.P., 1985. Seismic potential for large and great interplate earthquakes along the Chilean and southern Peruvian margins of South America: A quantitative reappraisal, *Journ. Geophys. Res.*, 90, 3589-3615.
- Nishenko, S.P., 1991. Circum-Pacific seismic potential: 1989-1999, Pageoph., 135, 169-259.
- Nishenko, S.P. and McCann, W.R., 1981. Seismic potential for the world's major plate boundaries: 1981. In: Earthquake Prediction, An International Review, Maurice Ewing Ser., Vol. 4, Simpson, D.W. and Richards, P.G., eds., American Geophys. Union, Washington D.C., 20-28.
- Papadimitriou, E.E., 1993. Long term earthquake prediction along the western coast of South and Central America based on a time predictable model, *Pageoph.*, 140, 301-316.
- Prince, R.A. and Scheweller, W.J., 1978. Dates, rates and angles of faulting in the Peru-Chile trench, *Nature*, 271, 743-745.
- Quezada, F.J., 1997. Seismic observation in Chile, Bull. Intern. Inst. Seismol. Earthq. Engin., 31, 243-259.
- Scordilis, E.M., 2006. Empirical Global Relations Converting M_s and m_b to Moment Magnitude, *Journ. Seismology*, 10(2), 225-236.
- Stein, S., Engeln, J.E., De Meto, C., Gordan, R.G., Woods, D.R., Lundgren, P., Argus, D., Quibble, D., Stein, C., Weistein, S. and Wiens, D.A., 1986. The Nazca South America convergence rate and the recurrence of the grate Chilean earthquake, *Geophys. Res. Lett.*, 13, 713-716.
- Suarez, G., Gagnepain, J., Cisternas, A., Hatzfeld, D., Molnar, P., Ocola, L., Roecker, S.W. and Viode, J.P., 1990. Tectonic deformation of the Andes and the configuration of the subducted slab in central Peru: results from a microseismic experiment, *Geophys. J. Intern.*, 103, 1-12.
- Tsapanos, T.M., 2001. The Markov model as a pattern for earthquakes recurrence in South America, Proc. of the 9th Intern. Congr., Athens, September 2001, 1611-1617.
- Tsapanos, T.M. and Burton, P.W., 1991. Seismic hazard evaluation for specific seismic regions of the world, *Tectonophysics*, 195, 153-169.
- Tsapanos, T.M. and Christova, C.V., 2000. Some preliminary results of the worldwide seismicity estimation: a case study of seismic hazard evaluation in South America, *Ann. di Geofis.*, 43, 11-22.